

Math 1553 Worksheet §3.4

1. True or false. Answer true if the statement is *always* true. Otherwise, answer false. If your answer is false, either give an example that shows it is false or (in the case of an incorrect formula) state the correct formula.
 - a) If A is an $n \times n$ matrix and the equation $Ax = b$ has at least one solution for each b in \mathbf{R}^n , then the solution is *unique* for each b in \mathbf{R}^n .
 - b) If A is a 3×4 matrix and B is a 4×2 matrix, then the linear transformation Z defined by $Z(x) = ABx$ has domain \mathbf{R}^3 and codomain \mathbf{R}^2 .

2. A is $m \times n$ matrix, B is $n \times m$ matrix. Select all correct answers from the box. It is possible to have more than one correct answer.

a) Suppose x is in \mathbf{R}^m . Then ABx must be in:

Col(A), Nul(A), Col(B), Nul(B)
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b) Suppose x in \mathbf{R}^n . Then BAX must be in:

Col(A), Nul(A), Col(B), Nul(B)
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c) If $m > n$, then columns of AB could be linearly

<i>independent</i> , <i>dependent</i>

d) If $m > n$, then columns of BA could be linearly

<i>independent</i> , <i>dependent</i>

3. Consider the following linear transformations:

$T: \mathbf{R}^3 \longrightarrow \mathbf{R}^2$ T projects onto the xy -plane, forgetting the z -coordinate

$U: \mathbf{R}^2 \longrightarrow \mathbf{R}^2$ U rotates clockwise by 90°

$V: \mathbf{R}^2 \longrightarrow \mathbf{R}^2$ V scales the x -direction by a factor of 2.

Let A, B, C be the matrices for T, U, V , respectively.

a) Write A , B , and C .

b) Compute the matrix for $U \circ V \circ T$.