

**Math 1553 Worksheet: Sections 5.1-5.2**

**1.** True or false: If  $v_1$  and  $v_2$  are linearly independent eigenvectors of an  $n \times n$  matrix  $A$ , then they must correspond to different eigenvalues.

**2.** In what follows,  $T$  is a linear transformation with matrix  $A$ . Find the eigenvectors and eigenvalues of  $A$  without doing any matrix calculations. (Draw a picture!)

a)  $T : \mathbf{R}^3 \rightarrow \mathbf{R}^3$  that projects vectors onto the  $xz$ -plane in  $\mathbf{R}^3$ .

b)  $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  that reflects vectors over the line  $y = 2x$  in  $\mathbf{R}^2$ .

3. True or False: Suppose  $A = \begin{pmatrix} 3 & 0 & 0 \\ 5 & 1 & 0 \\ -10 & 4 & 7 \end{pmatrix}$ . Then the characteristic polynomial of  $A$  is

$$\det(A - \lambda I) = (3 - \lambda)(1 - \lambda)(7 - \lambda).$$

4. Find the eigenvalues and a basis for each eigenspace of  $A = \begin{pmatrix} 2 & 3 & 1 \\ 3 & 2 & 4 \\ 0 & 0 & -1 \end{pmatrix}$ .