## Math 1553 Worksheet §§5.6-6.3

**1.** Courage Soda and Dexter Soda compete for a market of 210 customers who drink soda each day.

Today, Courage has 80 customers and Dexter has 130 customers. Each day:

70% of Courage Soda's customers keep drinking Courage Soda, while 30% switch to Dexter Soda.

40% of Dexter Soda's customers keep drinking Dexter Soda, while 60% switch to Courage Soda.

a) Write a stochastic matrix *A* and a vector *x* so that *Ax* will give the number of customers for Courage Soda and Dexter Soda (in that order) tomorrow. You do not need to compute *Ax*.

**b)** Find the steady-state vector for *A*.

**c)** Use your answer from (b) to determine the following: in the long run, roughly how many daily customers will Courage Soda have?

**2.** Let *W* be the set of all vectors in  $\mathbb{R}^3$  of the form (x, x - y, y) where *x* and *y* are real numbers.

**a)** Find a basis for  $W^{\perp}$ .

**b)** Let  $x = \begin{pmatrix} 2 \\ -2 \\ 1 \end{pmatrix}$ . Find the projection  $x_W$  of x onto the subspace W and the orthogonal projection  $x_{W^{\perp}}$  of x onto the subspace  $W^{\perp}$ .