Name:_____ Recitation Section:_____

Math 1553 Quiz 2, Spring 2020 (10 points, 10 minutes)
Jankowski, Lecture C1-C4 (11:15 AM)

Solutions

Show your work on problem 3 or you may receive little or no credit. You do not need to show work or justify your answers on problems 1 and 2.

1. (1 point each) Which of the following matrices are in RREF (reduced row echelon form)? Clearly circle all that apply.

a) $\begin{pmatrix} 1 & 7 & 0 \\ 0 & 0 & 1 \end{pmatrix}$

b) $\left(\begin{array}{cc|c} 1 & 1 & -1 \\ 0 & 0 & 1 \end{array}\right)$

The matrix in (a) is in RREF. However, (b) is not in RREF, since the pivot in the rightmost column has a nonzero entry above it.

2. (1 point each) Consider the augmented matrices below. For each matrix, determine whether the corresponding system of linear equations has no solution, exactly one solution, or infinitely many solutions. Clearly circle your answer.

a) $\left(\begin{array}{cccc|c} 1 & 0 & -2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{array}\right)$

[No solution] Exactly 1 solution Infinitely many solutions

b) $\left(\begin{array}{cc|c} 1 & 0 & -1 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{array}\right)$

No solution [Exactly 1 solution] Infinitely many solutions

Turn to the back side for problem 3!

3. (6 points) Consider the following system of linear equations:

$$x_1 - x_2 + x_3 = 1$$
$$2x_1 - 2x_2 + x_3 = 0$$
$$-x_1 + x_2 - x_3 = -1.$$

a) (3 points) Write the augmented matrix corresponding to the system, and put the matrix into RREF.

$$\left(\begin{array}{ccc|c} 1 & -1 & 1 & 1 \\ 2 & -2 & 1 & 0 \\ -1 & 1 & -1 & -1 \end{array}\right) \xrightarrow[R_3=R_3+R_1]{R_2=R_2-2R_1} \left(\begin{array}{ccc|c} 1 & -1 & 1 & 1 \\ 0 & 0 & -1 & -2 \\ 0 & 0 & 0 & 0 \end{array}\right) \xrightarrow[\text{then } R_1=R_1-R_2]{R_2=-R_2} \left(\begin{array}{ccc|c} 1 & -1 & 0 & -1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 \end{array}\right)$$

The pivots are highlighted in red above.

b) (3 points) Write the solution set to the system of equations in parametric form.

We see x_2 is free, and the equations from the RREF are

$$x_1 - x_2 = 1, \qquad x_2 = x_2 \quad (x_2 \text{ real}), \qquad x_3 = 2.$$

Thus,

$$\boxed{x_1 = 1 + x_2, \qquad x_2 = x_2 \quad (x_2 \text{ real}), \qquad x_3 = 2}.$$