

### Math 1553 Supplement, Chapter 7

1. True or false. If the statement is always true, answer true. Otherwise, answer false. Justify your answer.
  - a) Suppose  $W = \text{Span}\{w\}$  for some vector  $w \neq 0$ , and suppose  $v$  is a vector orthogonal to  $w$ . Then the orthogonal projection of  $v$  onto  $W$  is the zero vector.
  - b) Suppose  $W$  is a subspace of  $\mathbf{R}^n$  and  $x$  is a vector in  $\mathbf{R}^n$ . If  $x$  is not in  $W$ , then  $x - x_W$  is not zero.
  - c) Suppose  $W$  is a subspace of  $\mathbf{R}^n$  and  $x$  is in both  $W$  and  $W^\perp$ . Then  $x = 0$ .
  - d) Suppose  $\hat{x}$  is a least squares solution to  $Ax = b$ . Then  $\hat{x}$  is the closest vector to  $b$  in the column space of  $A$ .
  
2. Let  $W = \text{Span}\{v_1, v_2\}$ , where  $v_1 = \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix}$  and  $v_2 = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$ .
  - a) Find the closest point  $w$  in  $W$  to  $x = \begin{pmatrix} 0 \\ 14 \\ -4 \end{pmatrix}$ .
  
  - b) Find the distance from  $w$  to  $\begin{pmatrix} 0 \\ 14 \\ -4 \end{pmatrix}$ .
  
  - c) Find the standard matrix for the orthogonal projection onto  $\text{Span}\{v_1\}$ .
  
  - d) Find the standard matrix for the orthogonal projection onto  $W$ .