

Math 1553 Supplement, Chapter 7

1. True or false. If the statement is always true, answer true. Otherwise, answer false. Justify your answer.
 - a) Suppose $W = \text{Span}\{w\}$ for some vector $w \neq 0$, and suppose v is a vector orthogonal to w . Then the orthogonal projection of v onto W is the zero vector.
 - b) Suppose W is a subspace of \mathbf{R}^n and x is a vector in \mathbf{R}^n . If x is not in W , then $x - x_W$ is not zero.
 - c) Suppose W is a subspace of \mathbf{R}^n and x is in both W and W^\perp . Then $x = 0$.
 - d) Suppose \hat{x} is a least squares solution to $Ax = b$. Then \hat{x} is the closest vector to b in the column space of A .

2. Let $W = \text{Span}\{v_1, v_2\}$, where $v_1 = \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix}$ and $v_2 = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$.
 - a) Find the closest point w in W to $x = \begin{pmatrix} 0 \\ 14 \\ -4 \end{pmatrix}$.

 - b) Find the distance from w to $\begin{pmatrix} 0 \\ 14 \\ -4 \end{pmatrix}$.

 - c) Find the standard matrix for the orthogonal projection onto $\text{Span}\{v_1\}$.

 - d) Find the standard matrix for the orthogonal projection onto W .