#### MATH 1553, SPRING 2020 SAMPLE MIDTERM 3B: COVERS 4.1 THROUGH 5.6

Name	S	Section	

Please **read all instructions** carefully before beginning.

- Our actual midterm 3 will take place on Canvas, and you will have 75 minutes to complete it. Before the end of the day on Friday, April 10, Sample Midterm 3A will be posted on Canvas.
- This practice exam (3B) is meant to be completed in 50 minutes or less. It is meant as additional practice for our midterm.
- As always, RREF means "reduced row echelon form".

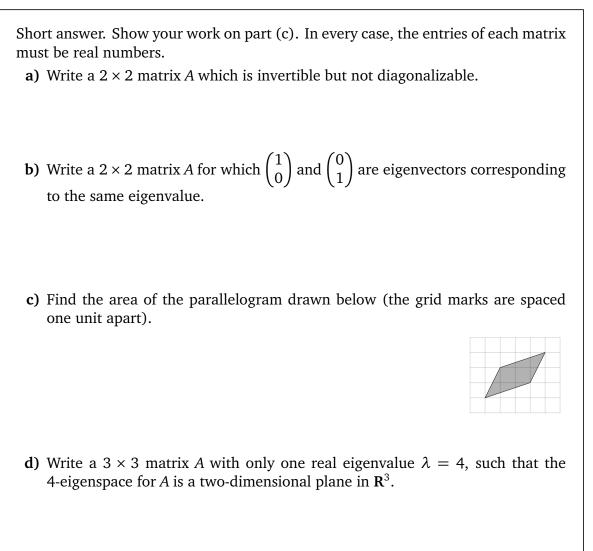
The exam is not designed to test material from the previous midterm on its own. However, knowledge of the material prior to section §4.1 is necessary for everything we do for the rest of the semester, so it is fair game for the exam as it applies to §§4.1 through 5.6. This page was intentionally left blank.

# Problem 1.

Answer true if the statement is <i>always</i> true. Otherwise, answer false. In every case, assume that the entries of the matrix <i>A</i> are real numbers.				
a)	Т	F	If <i>A</i> is the $3 \times 3$ matrix satisfying $Ae_1 = e_2$ , $Ae_2 = e_3$ , and $Ae_3 = e_1$ , then det( <i>A</i> ) = 1.	
b)	Т	F	If <i>A</i> is an $n \times n$ matrix and det( <i>A</i> ) = 2, then 2 is an eigenvalue of <i>A</i> .	
c)	Т	F	If <i>A</i> and <i>B</i> are $n \times n$ matrices with det( <i>A</i> ) = 0 and det( <i>B</i> ) = 0, then det( <i>A</i> + <i>B</i> ) = 0.	
d)	Т	F	If <i>A</i> is an $n \times n$ matrix and <i>v</i> and <i>w</i> are eigenvectors of <i>A</i> , then $v + w$ is also an eigenvector of <i>A</i> .	
e)	Т	F	It is possible for a lower-triangular matrix <i>A</i> to have a non-real complex eigenvalue.	

Extra space for scratch work on problem 1

#### Problem 2.



## Problem 3.

Parts (a) and (b) are unrelated.

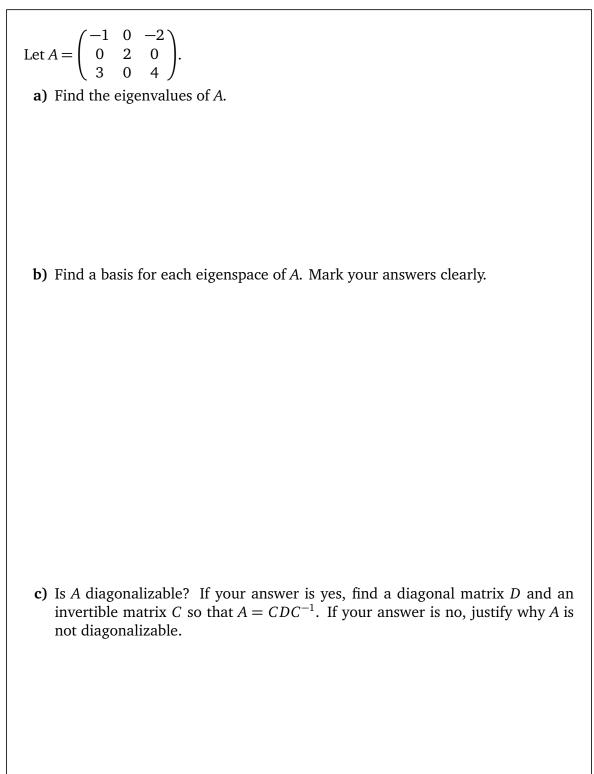
a) Consider the matrix

$$A = \begin{pmatrix} 3 & -7 \\ 1 & -1 \end{pmatrix}$$

Find all eigenvalues of *A*. Simplify your answer. For the eigenvalue with negative imaginary part, find an eigenvector.

**b)** Let  $A = \begin{pmatrix} 7 & -8 \\ 4 & -5 \end{pmatrix}$ . Find a formula for  $A^n$  and simplify your answer completely.

## Problem 4.



## Problem 5.

Parts (a) and (b) are not related.

**a)** Find det(
$$A^3$$
) if  $A = \begin{pmatrix} 1 & -3 & 4 & 2 \\ 0 & 0 & -2 & 0 \\ 0 & 1 & 2 & 3 \\ 2 & 0 & -1 & 20 \end{pmatrix}$ .

**b)** Find the  $2 \times 2$  matrix *A* whose eigenspaces are drawn below. Fully simplify your answer. (to be clear: the dashed line is the (-2)-eigenspace).

