MATH 1553, FALL 2019 SAMPLE MIDTERM 1B: COVERS THROUGH SECTION 2.5

Name	Section	

Please **read all instructions** carefully before beginning.

- Write your name on the front of each page (not just the cover page!).
- The maximum score on this exam is 50 points, and you have 50 minutes to complete this exam.
- There are no calculators or aids of any kind (notes, text, etc.) allowed.
- As always, RREF means "reduced row echelon form."
- Show your work, unless instructed otherwise. A correct answer without appropriate work will receive little or no credit! If you cannot fit your work on the front side of the page, use the back side of the page and indicate that you are doing so.
- We will hand out loose scrap paper, but it **will not be graded** under any circumstances. All work must be written on the exam itself.
- You may cite any theorem proved in class or in the sections we covered in the text.
- Good luck!

This is a practice exam. It is meant to be similar in format, length, and difficulty to the real exam. It is **not** meant as a comprehensive list of study problems. I recommend completing the practice exam in 50 minutes, without notes or distractions.

Scoring Page

Please do not write on this page.

1	2	3	4	5	Total

Problem 1.

In parts (c) and (e), *A* denotes an $m \times n$ matrix (*m* rows and *n* columns), and in (e), *b* is a vector in \mathbb{R}^m . In (b)–(e), circle **T** if the statement is necessarily true, and circle **F** otherwise.

a) What is the best way to describe the solution set of the equation x + 2y - z = 0?

a line in \mathbf{R}^2 a plane in \mathbf{R}^2 a line in \mathbf{R}^3 a plane in \mathbf{R}^3 Т F The following matrix has three pivots: b) $\begin{pmatrix}
1 & 7 & 2 & | & 4 \\
0 & 0 & 1 & | & -2 \\
0 & 0 & 0 & | & 15
\end{pmatrix}$ c) Т F It is possible for the matrix equation Ax = 0 to be inconsistent. Т F d) The following matrix corresponds to a linear system with one free variable: e) Т F The solution set of Ax = b is empty or it is a translate of a span in \mathbf{R}^m .

Problem 2.

Consider the following system of linear equations:

2x + y + 12z = 1x + 2y + 9z = -1.

a) [1 point] Write the system as a vector equation.

b) [1 point] Write the system as a matrix equation.

c) [1 point] Write the system as an augmented matrix.

d) [4 points] Find the solution set in parametric vector form.

e) [3 points] Draw a picture of the solution set.

Problem 3.

Consider the following vectors:

$$v_1 = \begin{pmatrix} 17 \\ -3 \\ 24 \end{pmatrix} \qquad v_2 = \begin{pmatrix} 7/2 \\ 0 \\ \pi \end{pmatrix}$$

a) [4 points] Describe Span{ v_1, v_2 } geometrically: "it is a in **R**."

b) [6 points] Find a matrix *A* with three rows, with the property that the matrix equation Ax = b is consistent if and only if *b* is in Span{ v_1, v_2 }.

a) Let
$$v_1 = \begin{pmatrix} 1 \\ 3 \\ 4 \\ 2 \end{pmatrix}$$
, $v_2 = \begin{pmatrix} 2 \\ 7 \\ 0 \\ 1 \end{pmatrix}$, and $v_3 = \begin{pmatrix} -1 \\ -5 \\ 12 \\ 4 \end{pmatrix}$. Is $\{v_1, v_2, v_3\}$ linearly independent?
If your answer is yes, justify why. If your answer is no, give a linear dependence relation for v_1 , v_2 , and v_3 .
b) Find a vector w in \mathbb{R}^3 that is not in Span $\left\{ \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right\}$. Is the set $\left\{ \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, w \right\}$ linearly independent? Justify your answer.



You needn't show your work in this problem.

[Scratch work]